

Dimensional Analysis HW 1: Hot Tub T-table

In this homework, we'll learn (or, for some of you, re-learn!) one of the most efficient ways to collecting numerical information: t-tables.

Here's an example. After filling up his hot tub, Sean looked at the thermometer on the side every hour and recorded the results.

| <u>Hours after Filling</u> | <u>Temperature (degrees Celsius)</u> |
|----------------------------|--------------------------------------|
| 0 | 9.2 |
| 1 | 12.2 |
| 2 | 15.0 |
| 3 | 18.2 |
| 4 | 21.1 |
| 5 | 24.1 |
| 6 | 26.9 |
| 7 | 29.7 |
| 8 | 32.4 |
| 9 | 35.2 |
| 10 | 40.4 |
| 11 | 39.9 |
| 12 | 40.3 |
| 13 | 39.9 |
| 14 | 40.1 |
| 15 | 40.2 |
| 16 | 40.3 |
| 17 | 40.1 |
| 18 | 40.2 |
| 19 | 40.4 |
| 20 | 40.0 |
| 21 | 40.2 |
| 22 | 40.0 |

1. **(1 point)** What temperature was the water when he first turned on the hot tub's heater? Make sure you include the correct unit!
2. **(2 points) (w)** Subtract the temperature that he recorded at hour 4 from the temperature he recorded at hour 7 (you should have a positive number – if not, subtract them the other way). Then divide that number by 3—since the hot tub heated up that many degrees over *three* hours. Write that **final** result below, with its correct unit. (Think carefully about the unit, and [check this video out](#) if you need help!)

The number you just calculated is the Average Rate of Change (AROC) of the water temperature in the hot tub between hours 4 and 7 (some of you may have called this “slope” in the past – they’re two different names for the same idea!).

The number you calculated “smooths out” the increase in temperature: you might notice that from hour 4 to 5, the tub increased by 3 degrees Celsius, but from hours 5 to 6, it only increased by 2.8 degrees Celsius (same as from hours 6 to 7). So the AROC aims to “smooth out” the change in the dependent variable (temperature) over a constant change in the independent variable (time).

3. **(1 point) (w)** What’s the AROC between hours 0 and 3? Include the correct unit.
4. **(1 point)** How does that AROC compare to the one from #2?
5. **(1 point) (w)** What’s the AROC between hours 2 and 10? Include the correct unit.
6. **(1 point)** How does that AROC compare to the one from #2 and #3?
7. **(1 point) (w)** What’s the AROC between hours 0 and 22? Include the correct unit.
8. **(2 points)** Why is that AROC so different than the others you calculated?